This chapter presents five example items within each of the mathematics content areas, including the performance on each of the items for each of the TIMSS countries. The example items in this chapter were chosen to illustrate the different topics covered within each content area as well as the different performance expectations. The items also were chosen to show the range of item formats used within each content area. To provide some sense of what types of items were answered correctly by higher-performing as compared to lower-performing students, the items show a range of difficulty within each content area. Finally, it should be noted that all these items and others are released for use by the public. ${ }^{1}$

The presentation for each of the content areas begins with a brief description of the major topics included in the content area, followed by a series of five tables showing achievement results on example items from that content area. Each table shows the percentages of correct responses on the example item for each of the TIMSS countries at both the third and fourth grades. If the item also was included in the TIMSS mathematics test at the seventh and eighth grades, it is so designated, and the international averages are shown for those grades for purposes of comparison. Each table also presents the example item in its entirety. The correct answer is circled for multiple-choice items and shown in the answer space for short-answer items. For extended-response questions, the answer shown exemplifies the type of student responses that were given full credit. All of the responses shown have been reproduced from students' actual test booklets.

After the tables showing the country-by-country results on each of the items, there is a figure relating achievement on each of the example items to performance on the TIMSS international mathematics scale. This "difficulty map" provides a pictorial representation of achievement on the scale in relation to achievement on the example items for the content area.

## What Have Students Learned About Whole Numbers?

The category of whole numbers included understanding place value through the thousands, ordering and comparing numbers, and solving single- as well as multi-step problems involving the operations of addition, subtraction, and multiplication. As shown by the results in Table 3.1, students in most countries demonstrated a basic understanding of the place value of whole numbers (Example Item 1). Students in the fourth grade, in particular, were successful on this item which required students to select the largest number when given four choices, all with four places but

[^0]differing in the third-, second-, and first-place values (international average of $86 \%$ compared to $76 \%$ for the lower grade students.) Differences in the ages at which students begin formal schooling and in curricular emphases appear to be reflected in the results. For example, more than $90 \%$ of both the third and fourth graders answered this question correctly in Japan and Korea. In Norway, where students begin school at a somewhat older age and thus have had fewer years of formal schooling, this question was answered correctly by $56 \%$ of the lower-grade students and $87 \%$ of those in the upper grade.

Table 3.2 presents Example Item 2, asking students to represent an addition fact as a multiplication fact. Students were required to provide a response rather than select an answer in the multiple-choice format. Both $5 \times 4=20$ and $4 \times 5=20$ were considered to be correct responses, as were equivalent written-out statements. As with the results for the item on comparing numbers, students at both grades did well in Hong Kong, Japan, Korea, and Singapore ( $86 \%$ or better). In most countries, however, the results were somewhat lower. As indicated by the international averages of $77 \%$ and $63 \%$, respectively, the fourth-grade students tended to perform more than 10 percentage points higher than the third-grade students.

Example Item 3 is a subtraction problem with whole numbers that requires regrouping (see Table 3.3). As noted at the bottom of the table, this item also was part of the mathematics test at seventh and eighth grades. The international averages of $86 \%$ at both the seventh and the eighth grades suggest that students in most countries had developed a grasp of how to solve this type of problem prior to the middle school years. In contrast, the results at the third and fourth grades were highly variable. For example, about $90 \%$ of the students at both grades answered correctly in Korea and Singapore. Considerable growth between grades was shown in most of the remaining countries. Despite this growth, however, in England and New Zealand fewer than 40\% of the fourth graders answered this question correctly.

Example Item 4 asked students to solve an addition number sentence involving whole numbers to different place values (one, two, three, and four places). As shown in Table 3.4, fourth-grade students were more successful than their third-grade counterparts in correctly answering this free-response question (international averages of $63 \%$ at fourth grade compared to $44 \%$ at third grade). Correct responses included either 700 or its equivalent written out as "seven hundred." In Korea and Singapore, more than $90 \%$ of the fourth graders provided the missing value necessary to make the sentence true.

Example Item 5 is the most difficult of the examples shown in the area of whole numbers. Students needed to recognize that compared to 24 multiplied by 18, multiplying 25 by 18 would increase the product by 18 . As shown in Table 3.5 , on average across countries, fewer than half the fourth graders ( $45 \%$ ) and one-third of the third graders ( $30 \%$ ) answered this question correctly. Fourth graders in Korea had the best performance ( $80 \%$ correct). Interestingly, increasing the product by 1 (option A) was by far the most popular distracter. Internationally, on average, it was selected by $35 \%$ of the fourth graders and $42 \%$ of the third graders.

Figure 3.1 presents a pictorial representation of the relationship between performance on the TIMSS international mathematics scale and achievement on the five example items for whole numbers. ${ }^{2}$ The international achievement on each example item is indicated both by the average percent correct across all countries at the third and fourth grades and by the international mathematics scale value, or item difficulty level, for each item. Since the scale was developed based on the performance of students at both grades in all countries, the international scale values apply to both grades and to all countries.

For the figure, the item results have been placed on the scale at the point where students at that level were more likely than not ( $65 \%$ probability) to answer the question correctly. For example, students scoring at or above 530 on the scale were likely to provide a correct response to the item asking for the missing value in the addition number sentence (Example Item 4), and those scoring at or above 614 were likely to respond correctly to the problem about the increase in the product when multiplying 18 by 25 rather than by 24 (Example Item 5). Considering that the international average on the scale was 529 at the fourth grade, however, students achieving at about the level of the international average were unlikely to have answered the latter item correctly. These results, however, varied dramatically by country. Fourth-grade students in Singapore, whose mean achievement was 625, had relatively high probabilities of answering all but the most difficult whole number items correctly. Indeed, this is borne out by Singapore's average percent correct of $83 \%$ in this content area at the fourth grade.

[^1]
## Table 3.1 Whole Numbers

## Percent Correct for Example Item 1 <br> Lower and Upper Grades (Third and Fourth Grades*)



[^2]
## Table 3.2 Whole Numbers

## Percent Correct for Example Item 2

Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Addition/multiplication fact. |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 58 (2.1) | 76 (1.7) |  |
| Cyprus | 63 (1.9) | 83 (1.5) |  |
| Czech Republic | 63 (2.2) | 83 (1.6) | $\square$ |
| ${ }^{\text {² }}$ England | 39 (2.0) | 53 (1.9) | Addition Fact |
| Greece | 58 (2.4) | 79 (1.9) | $4+4+4+4+4=20$ |
| Hong Kong | 89 (1.3) | 95 (0.9) |  |
| Iceland | 38 (2.6) | 63 (3.0) | Write this addition fact as a multiplication fact. |
| Iran, Islamic Rep. | 62 (2.0) | 73 (1.7) |  |
| Ireland | 74 (2.2) | 86 (1.6) | $4 \times 5=20$ |
| Japan | 86 (1.3) | 92 (0.8) |  |
| Korea | 91 (1.4) | 94 (0.9) |  |
| New Zealand | 45 (2.7) | 67 (2.5) |  |
| Norway | 36 (2.8) | 66 (2.5) |  |
| Portugal | 52 (2.8) | 65 (2.3) |  |
| ${ }^{\dagger}$ Scotland | 51 (2.3) | 66 (2.1) |  |
| Singapore | 87 (1.1) | 90 (0.8) |  |
| United States | 67 (2.3) | 84 (1.4) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 57 (2.4) | 71 (1.6) |  |
| Austria | 71 (2.6) | 82 (1.7) |  |
| ${ }^{1}$ Latvia (LSS) | 66 (2.5) | 81 (2.0) |  |
| Netherlands | 78 (1.8) | 85 (1.5) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix |  |  |  |
| Slovenia | 69 (2.3) | 86 (1.5) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 61 (2.3) | 80 (1.4) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 86 (1.4) |  |
| Kuwait | -- | 42 (1.9) |  |
| Thailand | 54 (2.7) | 65 (2.2) |  |
| International Average Percent Correct | 63 (0.5) | 77 (0.4) |  |

[^3]
## Table 3.3 Whole Numbers

## Percent Correct for Example Item 3 <br> Lower and Upper Grades (Third and Fourth Grades*)



[^4]Table 3.4 Whole Numbers
Percent Correct for Example Item 4
Lower and Upper Grades (Third and Fourth Grades*)


[^5]
## Table 3.5 Whole Numbers

Percent Correct for Example Item 5
Lower and Upper Grades (Third and Fourth Grades*)


[^6]
## International Difficulty Map for Whole Numbers Example Items Lower and Upper Grades (Third and Fourth Grades*)



[^7]
## What Have Students Learned About Fractions and Pro portionality?

Within the content area of fractions and proportionality, students were asked to recognize the pictorial representation of common fractions and decimal fractions as well as the relationships between common and decimal fractions. Several items involved addition and subtraction with fractions and decimals. This content area also included several word problems that could be solved with proportionality and one item involving scale on a map. As indicated in Chapter 2, the items in this content area tended to be more difficult for students than those in the other content areas. For example, the international average across countries in the content area of whole numbers was $66 \%$ compared to an average of $48 \%$ in the content area of fractions and proportionality.

In the least difficult of the example items, Example Item 6, students were asked to recognize that five-ninths of the figure was shaded. As shown in Table 3.6, about half the students internationally selected the correct response ( $61 \%$, on average, at the fourth grade and $42 \%$ at the third grade). There was a considerable range of performance on this item, however. For example, more than $90 \%$ of the fourth-grade students answered this question correctly in Hong Kong, Korea, and Singapore. Five-fourths (option A) was the most commonly selected wrong answer. On average, it was indicated by $28 \%$ of the students at the third grade and $23 \%$ at the fourth grade. Presumably, these students took the fraction to represent five shaded squares and four unshaded squares.

Example Item 7, a multiple-choice word problem where students could have used proportional reasoning, asked how much sauce could be made from 15 tomatoes if five tomatoes yielded one-half of a liter of sauce. As shown in Table 3.7, approximately one-half of the fourth- and third-grade students internationally answered this question correctly ( $53 \%$ and $42 \%$, respectively.) The results were generally uniform across countries, with about $40 \%$ to $60 \%$ of the fourth graders providing correct responses in most countries. Somewhat more than $60 \%$ of the fourth graders provided correct responses in Hong Kong (73\%), Korea (67\%), and the Netherlands (67\%). Internationally, about one-fourth of both the third and fourth graders selected the answer of three liters (option D), indicating that they grasped the 1 to 3 ratio, but not the fractional unit of measure.

On Example Item 8, requiring students to recognize that 0.2 represented the shaded part of the figure, the international averages for the correct answer were $40 \%$ and $33 \%$ at the fourth and third grades, respectively. In comparison, internationally, on average, $44 \%$ of the fourth-grade students and $43 \%$ of the third-grade students selected 2.8 (option A) as their answer. Similar to the misconception about fractional representation shown in Example 6, in this item, many students chose the representation that seemed to suggest two shaded and eight unshaded parts of the figure.

Example Item 9 is a word problem involving subtraction of decimals. As shown in Table 3.9, this problem was extremely difficult for students in many countries (international averages of $26 \%$ at fourth grade and $12 \%$ at third grade). Korea and Singapore were the only two countries where the majority of the fourth graders provided the completely correct response of 63.2 together with their calculation of 96.4-33.2 or its equivalent. (On average across countries, approximately $10 \%$ of the fourth-grade students and $8 \%$ of the third-grade students received partial credit for providing the correct answer but not showing an acceptable description or calculation.)

In Example Item 10, students were asked to explain their answers using words and pictures (see Table 3.10). For the first part of the question, students needed to express verbally, symbolically, or pictorially that 20 is twice as much as 10 , or that 10 is half of 20 . As indicated by the sample response, many students drew diagrams or pictographs to explain why Juanita was right. The percentage of correct responses includes both those students who agreed that Juanita was right as well as the very few students (less than $1 \%$ in any country) who provided satisfactory explanations but gave neither a "yes" or "no" answer regarding whether Juanita was right. For the second part of this question, students were to express verbally, symbolically, or pictorially that 10 is not half of 30 . Students were to answer "no" to the question of whether Amanda was right, but a correct explanation received full credit when neither a "yes" or "no" answer was given. Both parts of this item were very difficult for students. The international averages for Part A were $10 \%$ and $21 \%$, respectively, for third and fourth graders. Thirty percent or more of the fourth graders provided fully correct answers in Australia, England, Japan, Korea, the Netherlands, and Singapore. On part B, the international averages were $6 \%$ for third-grade students and $15 \%$ for fourth-grade students. Thirty percent or more of the fourth graders provided fully correct responses in Japan, Korea, and Singapore.

The item difficulty map for fractions and proportionality is shown in Figure 3.2. The least difficult items involved whole-number proportional reasoning and recognizing the shaded parts of a rectangle representing a fraction. In contrast, the more difficult items involved decimals, or required students to explain their reasoning through words and diagrams.

# Table 3.6 Fractions and Proportionality 

## Percent Correct for Example Item 6

Lower and Upper Grades (Third and Fourth Grades*)


[^8]
## Table 3.7 Fractions and Proportionality

## Percent Correct for Example Item 7

Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 7Sauce from 15 tomatoes. |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 33 (2.5) | 41 (2.3) | Mario uses 5 tomatoes to make half a liter of tomato sauce. How much sauce can he make from 15 tomatoes? |
| Cyprus | 46 (2.8) | 51 (3.0) |  |
| Czech Republic | 50 (2.4) | 64 (2.9) |  |
| ${ }^{+2}$ England | 39 (2.9) | 51 (3.0) | (A.) A liter and a half <br> B. Two liters <br> C. Two liters and a half <br> D. Three liters |
| Greece | 45 (2.8) | 50 (3.2) |  |
| Hong Kong | 61 (1.8) | 73 (2.7) |  |
| Iceland | 34 (3.7) | 44 (3.8) |  |
| Iran, Islamic Rep. | 35 (3.3) | 44 (2.7) |  |
| Ireland | 41 (2.9) | 56 (2.5) |  |
| Japan | 37 (2.5) | 45 (2.4) |  |
| Korea | 53 (2.7) | 67 (2.5) |  |
| New Zealand | 37 (3.0) | 48 (3.6) |  |
| Norway | 33 (2.6) | 51 (3.0) |  |
| Portugal | 37 (2.7) | 42 (3.2) |  |
| ${ }^{\dagger}$ Scotland | 29 (2.4) | 46 (2.5) |  |
| Singapore | 51 (2.1) | 60 (2.2) |  |
| United States | 37 (3.3) | 43 (2.0) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 49 (2.9) | 59 (2.6) |  |
| Austria | 42 (3.3) | 51 (3.0) |  |
| ${ }^{1}$ Latvia (LSS) | 37 (3.5) | 53 (3.3) |  |
| Netherlands | 42 (2.5) | 67 (3.2) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 48 (3.2) | 61 (3.2) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 52 (2.7) | 60 (2.5) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 60 (2.9) |  |
| Kuwait | -- | 23 (2.3) |  |
| Thailand | 46 (3.5) | 57 (2.7) |  |
| International Average Percent Correct | 42 (0.6) | 53 (0.6) |  |

[^9]
## Table 3.8 Fractions and Proportionality

## Percent Correct for Example Item 8 <br> Lower and Upper Grades (Third and Fourth Grades*)



[^10]
## Table 3.9 Fractions and Proportionality

## Percent Correct for Example Item 9 Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 9 |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 9 (1.2) | 25 (2.2) | Julie put a box on a shelf that is 96.4 centimeters long. The box is 33.2 centimeters long. What is the longest box she could put on the rest of the shelf? Show all your work. |
| Cyprus | 3 (0.7) | 16 (1.4) |  |
| Czech Republic | 16 (1.6) | 38 (1.9) |  |
| ${ }^{+2}$ England | 9 (1.3) | 22 (2.0) |  |
| Greece | 8 (1.6) | 21 (2.0) |  |
| Hong Kong | 20 (2.6) | 32 (2.1) | $\text { Answer: 63.2 cimelox } \frac{-36.2}{96}$ |
| Iceland | 1 (0.6) | 6 (1.1) |  |
| Iran, Islamic Rep. | 1 (0.4) | 9 (2.3) |  |
| Ireland | 12 (1.5) | 29 (1.9) |  |
| Japan | 26 (1.4) | 40 (1.9) |  |
| Korea | 34 (1.9) | 53 (2.0) |  |
| New Zealand | 3 (0.8) | 13 (1.9) |  |
| Norway | 3 (0.8) | 19 (1.8) |  |
| Portugal | 8 (1.3) | 15 (1.3) |  |
| ${ }^{\dagger}$ Scotland | 8 (1.2) | 27 (2.2) |  |
| Singapore | 46 (1.7) | 61 (1.6) |  |
| United States | 11 (1.3) | 32 (1.8) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 8 (1.1) | 23 (1.3) |  |
| Austria | 7 (1.5) | 31 (2.2) |  |
| ${ }^{1}$ Latvia (LSS) | 8 (1.4) | 18 (2.4) |  |
| Netherlands | 8 (1.0) | 28 (2.2) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 14 (1.6) | 33 (2.5) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 5 (0.9) | 13 (1.5) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 25 (1.9) |  |
| Kuwait | -- | 5 (0.7) |  |
| Thailand | 23 (3.7) | 32 (2.7) |  |
| International Average Percent Correct | 12 (0.3) | 26 (0.4) |  |

[^11]
## Table 3.10 Fractions and Proportionality

## Percent Correct for Example Item 10A <br> Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Girl/Boy ratio: ls Juanita right? |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 10 (1.2) | 22 (1.7) | There are 10 girls and 20 boys in Juanita's class. Juanita said that there is one girl for every two boys. Her friend Amanda said that means $\frac{1}{2}$ of all the students in the class are girls. |
| Cyprus | 5 (1.0) | 21 (1.6) |  |
| Czech Republic | 9 (1.2) | 25 (1.5) |  |
| ${ }^{+2}$ England | 17 (1.2) | 30 (1.8) |  |
| Greece | 7 (1.6) | 11 (1.4) |  |
| Hong Kong | 3 (0.6) | 11 (2.0) | How many students are there in Juanita's class. Answer: 30 |
| Iceland | 2 (0.7) | 5 (1.2) |  |
| Iran, Islamic Rep. | 3 (0.7) | 7 (1.2) | Is Juanita right? Answer: $\qquad$ yes <br> Use words or pictures to explaih why. <br> gir |
| Ireland | 12 (1.4) | 26 (1.9) |  |
| Japan | 12 (0.9) | 30 (1.6) | Boys pog9090000002 |
| Korea | 31 (1.7) | 43 (2.4) | O o piofopopo |
| New Zealand | 14 (1.6) | 25 (2.5) | $\left(\begin{array}{l}\text { (xittittita }) \\ (0) \text { groups of two }\end{array}\right.$ |
| Norway | 8 (1.4) | 24 (2.1) |  |
| Portugal | 4 (0.8) | 9 (1.1) | Is Amanda right? Answer: $\qquad$ Use words and pictures to explain why |
| ${ }^{\dagger}$ Scotland | 11 (1.3) | 26 (1.9) |  |
| Singapore | 26 (1.9) | 41 (1.9) |  |
| United States | 13 (1.6) | 25 (1.5) | because 1 - 15 not 10 |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  | and itis not $\partial$ |
| Australia | 21 (2.0) | 34 (1.6) | ) boys |
| Austria | 3 (0.9) | 13 (1.5) |  |
| ${ }^{1}$ Latvia (LSS) | 3 (0.7) | 9 (1.5) |  |
| Netherlands | 16 (1.7) | 38 (2.3) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 9 (1.6) | 24 (2.5) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | -- | - - |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 19 (1.7) |  |
| Kuwait | - - | 7 (1.0) |  |
| Thailand | 0 (0.2) | 4 (1.3) |  |
| International Average Percent Correct | 10 (0.3) | 21 (0.4) |  |

[^12]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## Table 3.10 Fractions and Proportionality (Continued)

## Percent Correct for Example Item 10B <br> Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 10BGirl/Boy ratio: Is Amanda right? |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 3 (0.6) | 12 (1.5) | There are 10 girls and 20 boys in Juanita's class. Juanita said that there is one girl for every two boys. Her friend Amanda said that means $\frac{1}{2}$ of all the students in the class are girls. |
| Cyprus | 3 (0.8) | 12 (1.2) |  |
| Czech Republic | 5 (1.1) | 18 (1.7) |  |
| ${ }^{\dagger 2}$ England | 9 (1.0) | 20 (1.3) |  |
| Greece | 1 (0.5) | 8 (1.2) |  |
| Hong Kong | 4 (0.7) | 13 (2.0) | How many students are there in Juanita's class. Answer: 30$\qquad$ |
| Iceland | 0 (0.3) | 5 (1.1) |  |
| Iran, Islamic Rep. | 0 (0.3) | 1 (0.4) | Is Juanita right? Answer: yes <br> Use words or pictures to explain why. $\qquad$ <br> gir/s <br> 000000 $\text { Boys } 069090002000$ |
| Ireland | 9 (1.5) | 25 (1.9) |  |
| Japan | 10 (1.0) | 30 (1.5) |  |
| Korea | 20 (1.6) | 32 (2.0) |  |
| New Zealand | 7 (1.0) | 15 (1.6) | (xittittita 10 groups of two |
| Norway | 6 (1.1) | 15 (1.7) |  |
| Portugal | 1 (0.4) | 3 (0.6) | Is Amanda right? Answer: $\quad$ n 0 <br> Use words and pictures to explain why. $\begin{aligned} & \text { because } \frac{1}{2} \text { is } 15 \text { not } 10 \mathrm{girls} \\ & \text { and itis not } 20 \text { boys } \end{aligned}$ |
| ${ }^{\dagger}$ Scotland | 6 (1.0) | 16 (1.7) |  |
| Singapore | 22 (1.8) | 37 (2.0) |  |
| United States | 6 (1.1) | 17 (1.5) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 11 (1.2) | 21 (1.6) |  |
| Austria | 2 (1.0) | 5 (1.0) |  |
| ${ }^{1}$ Latvia (LSS) | 1 (0.4) | 6 (1.2) |  |
| Netherlands | 8 (1.0) | 24 (2.1) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 2 (0.7) | 12 (1.7) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | -- | -- |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 16 (1.7) |  |
| Kuwait | -- | 4 (0.8) |  |
| Thailand | 0 (0.2) | 4 (1.3) |  |
| International Average Percent Correct | 6 (0.2) | 15 (0.3) |  |

[^13]International Difficulty Map for Fractions and Proportionality Example Items Lower and Upper Grades (Third and Fourth Grades*)


[^14]
## What Have Students Learned About Measurement, Estimation, and Number Sense?

In the content area of measurement, estimation, and number sense, students were asked to demonstrate their understanding of common measures of length, area, volume, time, the calendar, temperature, and weight. Several questions involved rounding and estimation.

As shown in Example Item 11, students were asked to estimate the length of a pencil in centimeters. The international averages were $77 \%$ for fourth graders and $69 \%$ for third graders (see Table 3.11). More than half the third- and fourth-grade students in each country answered correctly, except the third graders in the United States ( $46 \%$ ), which was the only participating country that does not use the metric system. Because understanding the metric system is a goal of mathematics education in the United States, it used the international version of the measurement items related to the metric system rather than changing these items to reflect the more commonly used measures for length and volume.

Students at both grades also did relatively well on Example Item 12, asking them to select the largest mass given choices ranging from 1 milligram to 1 kilogram. The international averages were $72 \%$ for fourth-grade students and $61 \%$ for third-grade students. As shown in Table 3.12, $90 \%$ or more of the fourth graders answered correctly in Japan, Korea, the Netherlands, and Hungary.

When asked to estimate the total weight of 1000 clothespins each weighing 9.2 grams, students in a number of countries had some difficulty. The international averages on Example Item 13 were $55 \%$ for fourth graders and $41 \%$ for third graders. As shown in Table 3.13, performance was relatively uniform across countries, ranging at the fourth grade from $74 \%$ in the Czech Republic to $38 \%$ in Iran, with many countries in the $40 \%$ to $60 \%$ area.

When asked to apply their knowledge of milliliters in Example Item 14, most students did not recognize that liquid in a teaspoon would be measured in this unit (international averages of $38 \%$ and $30 \%$ ). Perhaps surprisingly, about one-fourth of the students internationally did not seem to recognize that milliliters could not be used to measure thickness. Options C and D were equally popular distracters (both were selected by $23 \%$ of the students at grade 4). However, more than $70 \%$ of the fourth-grade students in Hong Kong ( $73 \%$ ) and Japan ( $75 \%$ ) answered this question correctly. The increases from third to fourth grade on this item were relatively small in most countries. One exception, however, was Hong Kong (from $41 \%$ to $73 \%$ ).

Example Item 15 is a multi-step problem requiring students to apply their understanding of the perimeter of rectangles. As shown by the results in Table 3.15, this item was very difficult for both third- and fourth-grade students. Both grades performed very similarly, as indicated by the international averages of $23 \%$ and $21 \%$. The largest increase and the best performance at the fourth grade was by the students in Singapore, from $19 \%$ to $46 \%$.

The international difficulty map for the measurement items is presented in Figure 3.3. It indicates that only the students with higher-than-average mathematics scores internationally were likely to demonstrate that they could go beyond a knowledge of basic weights and lengths to apply measurement skills in various situations.

## Table 3.11 Measurement, Estimation, and Number Sense

## Percent Correct for Example Item 11 <br> Lower and Upper Grades (Third and Fourth Grades*)



[^15]Table 3.12 Measurement, Estimation, and Number Sense
Percent Correct for Example Item 12
Lower and Upper Grades (Third and Fourth Grades*)


[^16]
## Table 3.13 Measurement, Estimation, and Number Sense

Percent Correct for Example Item 13
Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 13Best estimate of clothespin mass. |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |  |
| Canada | 42 (2.8) | 50 (2.3) | The weight (mass) of a clothespin is 9.2 g . Which of these is the best estimate of the total weight (mass) of 1000 clothespins? |  |
| Cyprus | 32 (2.5) | 44 (2.7) |  |  |
| Czech Republic | 50 (2.8) | 74 (2.5) |  |  |
| ${ }^{\dagger 2}$ England | 42 (2.8) | 47 (2.9) | A. $\quad 900 \mathrm{~g}$ <br> C. $\quad 90000 \mathrm{~g}$ <br> D. 900000 g |  |
| Greece | 27 (3.3) | 55 (2.9) |  |  |
| Hong Kong | 57 (2.5) | 71 (2.6) |  |  |
| Iceland | 32 (3.5) | 44 (2.9) |  |  |
| Iran, Islamic Rep. | 29 (2.5) | 38 (2.8) |  |  |
| Ireland | 40 (3.2) | 52 (2.6) |  |  |
| Japan | - - | - - |  |  |
| Korea | 64 (2.5) | 67 (2.5) |  |  |
| New Zealand | 39 (3.4) | 42 (2.8) |  |  |
| Norway | 27 (2.9) | 49 (3.1) |  |  |
| Portugal | 34 (3.4) | 43 (2.4) |  |  |
| ${ }^{+}$Scotland | 40 (2.8) | 50 (2.7) |  |  |
| Singapore | 55 (2.0) | 59 (2.5) |  |  |
| United States | 38 (2.6) | 52 (2.6) |  |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |  |
| Australia | 45 (2.5) | 53 (2.3) |  |  |
| Austria | 44 (3.6) | 65 (2.9) |  |  |
| ${ }^{1}$ Latvia (LSS) | 34 (3.2) | 57 (3.3) |  |  |
| Netherlands | 45 (2.8) | 71 (3.0) |  |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |  |
| Slovenia | 42 (2.5) | 71 (2.6) |  |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |  |
| Hungary | 48 (3.1) | 71 (2.4) |  |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |  |
| ${ }^{1}$ Israel | -- | 62 (2.4) |  |  |
| Kuwait | -- | 45 (2.7) |  |  |
| Thailand | 45 (3.3) | 50 (3.3) |  |  |
| International Average Percent Correct | 41 (0.6) | 55 (0.5) |  |  |

[^17]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## Table 3.14 Measurement, Estimation, and Number Sense

## Percent Correct for Example Item 14

Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Substance measured in mililiters. |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 31 (2.4) | 31 (2.7) | Which of these would most likely be measured in milliliters? |
| Cyprus | 21 (2.3) | 20 (2.9) |  |
| Czech Republic | 28 (2.3) | 32 (2.5) |  |
| ${ }^{+2}$ England | 30 (2.5) | 37 (2.8) | A. The amount of liquid in a teaspoon |
| Greece | 21 (2.6) | 27 (3.6) |  |
| Hong Kong | 41 (2.4) | 73 (2.3) | B. The weight (mass) of a pin |
| Iceland | 29 (3.4) | 29 (3.1) | C. The amount of gasoline in a tank |
| Iran, Islamic Rep. | 22 (3.0) | 26 (3.1) | C. The amount of gasoline in a tank |
| Ireland | 28 (2.1) | 44 (2.8) | D. The thickness of 10 sheets of paper |
| Japan | 62 (2.0) | 75 (1.8) |  |
| Korea | 25 (2.2) | 31 (2.5) |  |
| New Zealand | 22 (2.5) | 35 (3.6) |  |
| Norway | 21 (2.9) | 24 (2.1) |  |
| Portugal | 31 (2.3) | 45 (3.1) |  |
| ${ }^{\dagger}$ Scotland | 27 (2.3) | 35 (2.2) |  |
| Singapore | 39 (2.3) | 45 (1.9) |  |
| United States | 33 (2.8) | 38 (2.2) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 31 (3.0) | 44 (2.3) |  |
| Austria | 43 (3.5) | 51 (3.0) |  |
| ${ }^{1}$ Latvia (LSS) | 29 (3.5) | 42 (3.0) |  |
| Netherlands | 21 (2.0) | 27 (2.9) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 35 (2.8) | 45 (3.2) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 41 (2.9) | 55 (2.6) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 28 (3.1) |  |
| Kuwait | -- | 15 (1.6) |  |
| Thailand | 12 (2.1) | 22 (2.4) |  |
| International Average Percent Correct | 30 (0.5) | 38 (0.5) |  |

[^18]Table 3.15 Measurement, Estimation, and Number Sense
Percent Correct for Example Item 15
Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 15Length of rectangle. |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 19 (1.9) | 23 (2.4) | A thin wire 20 centimeters long is formed into a rectangle. If the width of this rectangle is 4 centimeters, what is its length? <br> A. 5 centimeters |
| Cyprus | 25 (2.5) | 28 (2.5) |  |
| Czech Republic | 15 (1.8) | 16 (1.8) |  |
| ${ }^{+2}$ England | 21 (2.6) | 29 (3.2) |  |
| Greece | 16 (2.2) | 16 (2.6) |  |
| Hong Kong | 20 (1.8) | 29 (1.9) | B. 6 centimeters <br> C. 12 centimeters <br> D. 16 centimeters |
| Iceland | 21 (2.7) | 12 (1.9) |  |
| Iran, Islamic Rep. | 13 (2.0) | 16 (2.2) |  |
| Ireland | 25 (2.3) | 20 (1.9) |  |
| Japan | 33 (2.2) | 32 (2.2) |  |
| Korea | 37 (2.6) | 38 (3.0) |  |
| New Zealand | 25 (2.4) | 23 (2.3) |  |
| Norway | 18 (2.7) | 19 (2.2) |  |
| Portugal | 19 (2.3) | 18 (2.2) |  |
| ${ }^{\dagger}$ Scotland | 26 (2.6) | 24 (1.9) |  |
| Singapore | 19 (1.4) | 46 (2.0) |  |
| United States | 25 (2.7) | 23 (1.9) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 24 (2.6) | 23 (2.1) |  |
| Austria | 25 (4.1) | 23 (2.3) |  |
| ${ }^{1}$ Latvia (LSS) | 19 (2.7) | 24 (3.1) |  |
| Netherlands | 31 (2.8) | 35 (3.6) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 11 (1.8) | 20 (2.3) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 13 (1.8) | 15 (2.0) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 17 (2.5) |  |
| Kuwait | -- | 22 (1.9) |  |
| Thailand | 12 (2.1) | 15 (2.4) |  |
| International Average Percent Correct | 21 (0.5) | 23 (0.5) |  |

[^19]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## International Difficulty Map for Measurement, Estimation, and Number Sense Example Items - Lower and Upper Grades (Third and Fourth Grades*)


*Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country. NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

## What Have Students Learned About Data Representation, Analysis, and Probability?

Example Items 16 through 20 illustrate the types of items that were asked about data representation, analysis, and probability. Most of the items in this content area required students to read and use data presented in a variety of charts, tables, and graphs. One task asked them to complete a bar graph from tabular data (Example 20). Two questions dealt with the basic concepts underlying probability (Examples 16 and 18).

Internationally, approximately three-fourths of the fourth graders and two-thirds of the third graders correctly answered Example Item 16 (see Table 3.16). More than $80 \%$ of the fourth-grade students in many of the countries appeared to understand that the target with the greatest shaded space had the best chance of being hit.

As shown in Table 3.17, students had little difficulty reading basic information from a bar graph of daily cartons of milk sold at a school, even though some simple interpolation was required to determine that 25 cartons of milk were sold on Monday (see Example Item 17A). The results indicate that this activity was familiar to students in nearly all countries, except Iran and Kuwait. The international averages were $75 \%$ and $60 \%$, respectively, at the two grades tested. Students had more difficulty with the second part of this free-response item, when they were asked to provide the number of cartons of milk sold all week and to show their work (see Example Item 17B). International averages on this part of the item decreased to $37 \%$ for fourth graders and $19 \%$ for third graders. To receive full credit, students needed to give the answer of 125 as well as show their calculation or provide a description of the procedure used. The fourth graders in Singapore had the best performance, providing 80\% correct responses.

Example Item 18 assessed the area of probability. In general, about one-half of the fourth-grade students appeared to understand that the probability of picking the one red marble was highest for the bag with the fewest number of marbles. Table 3.18 shows that the international averages were $40 \%$ and $51 \%$ at the third and fourth grades, respectively. Fifty percent or more of the students at both grades answered this question correctly in Japan, the United States, Australia, and the Netherlands. This item also was part of the TIMSS mathematics test given to seventh- and eighth-grade students. In comparison to performance at the primary grades, the international averages were $74 \%$ and $78 \%$ at the seventh and eighth grades, respectively. Fourth graders in the Netherlands did particularly well on this item, performing at about the international average for seventh grade.

Performance across countries varied on Example Item 19, which required students to interpret information shown in a pictograph (see Table 3.19). Essentially, this free-response question asked students to determine the key for the graph given the total number of cedar and hemlock trees. That is, students needed to communicate that each tree symbol represented 100 trees. The international averages were $49 \%$ and $34 \%$ at the fourth and third grades, respectively, indicating growth between the two grades in many countries. Most notably, in the Netherlands performance
increased from $30 \%$ to $63 \%$ correct. Variation in performance ranged from $85 \%$ or more of the students in Japan answering correctly at both grades to fewer than $20 \%$ answering correctly in Iran and Kuwait.

As shown in Table 3.20, Example Item 20 required students to complete a bar graph of the ages of boys and girls from data presented in a chart. To receive full credit, all four bars needed to be drawn to the appropriate heights. There could be a shading or placement problem in one set of the bars (i.e., for age 9 or age 10). The international averages were $41 \%$ at the fourth grade and $24 \%$ at the third grade. Seventy percent or more of the fourth graders in Hong Kong (75\%), Japan (78\%), Korea (83\%), and Singapore ( $74 \%$ ) received full credit for their bar graphs. The next highest performance was in the United States, where $55 \%$ of the fourth graders completed the graph according to the requirements. Internationally, on average, approximately $15 \%$ of the students received partial credit for having at least one bar completely correct, or the height of all four bars correct with multiple errors in placement or shading.

The item difficulty map presented in Figure 3.4 indicates that students had some difficulty moving beyond a straightforward reading of data in tables to actually using the data in calculations or to representing the data. Only students performing above the international average were likely to answer such questions correctly (Example ${ }^{\circ}$ highest probability of hitting a target with the largest shaded area. In contrast, fewer than half answered that the probability of picking the one red marble from a bag of marbles is highest for the bag with the fewest number of marbles.

Table 3.16 Data Representation, Analysis, and Probability
Percent Correct for Example Item 16
Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 16 |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 68 (2.4) | 83 (1.9) | Samantha drops a stone onto each of these targets. The stone has the best chance of landing on a shaded space in which target? |
| Cyprus | 55 (3.2) | 68 (2.5) |  |
| Czech Republic | 78 (2.2) | 82 (1.9) |  |
| ${ }^{+2}$ England | 73 (2.3) | 78 (1.9) |  |
| Greece | 73 (2.8) | 84 (2.0) | A. <br> (B.) <br> C. <br> D. |
| Hong Kong | 75 (1.7) | 84 (1.9) |  |
| Iceland | 62 (3.3) | 76 (3.2) |  |
| Iran, Islamic Rep. | 50 (3.6) | 70 (2.7) |  |
| Ireland | 66 (2.8) | 72 (2.5) |  |
| Japan | 89 (1.2) | 89 (1.5) |  |
| Korea | 81 (2.1) | 84 (2.0) |  |
| New Zealand | 61 (3.2) | 74 (2.8) |  |
| Norway | 70 (3.3) | 86 (2.3) |  |
| Portugal | 41 (3.0) | 62 (2.7) |  |
| ${ }^{\dagger}$ Scotland | 66 (2.6) | 73 (2.9) |  |
| Singapore | 60 (2.2) | 70 (1.8) |  |
| United States | 75 (2.5) | 83 (1.5) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 71 (3.3) | 79 (1.9) |  |
| Austria | 71 (3.3) | 81 (2.7) |  |
| ${ }^{1}$ Latvia (LSS) | 72 (3.2) | 79 (3.0) |  |
| Netherlands | 80 (2.3) | 86 (2.4) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 71 (2.3) | 84 (2.2) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 69 (2.5) | 76 (2.3) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 85 (2.7) |  |
| Kuwait | -- | 58 (1.9) |  |
| Thailand | 69 (3.3) | 78 (3.0) |  |
| International Average Percent Correct | 69 (0.6) | 78 (0.5) |  |

[^20]Table 3.17 Data Representation, Analysis, and Probability

## Percent Correct for Example Item 17A Lower and Upper Grades (Third and Fourth Grades*)



[^21]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## Table 3.17 Data Representation, Analysis, and Probability (Continued)

## Percent Correct for Example Item 17B <br> Lower and Upper Grades (Third and Fourth Grades*)



[^22]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

Table 3.18 Data Representation, Analysis, and Probability

## Percent Correct for Example Item 18 Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  |
| :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |
| Canada | 49 (3.0) | 63 (3.0) |
| Cyprus | 20 (2.5) | 32 (2.8) |
| Czech Republic | 42 (2.5) | 56 (2.5) |
| ${ }^{\dagger 2}$ England | 41 (2.5) | 55 (2.9) |
| Greece | 21 (2.5) | 30 (3.0) |
| Hong Kong | 45 (2.0) | 69 (3.1) |
| Iceland | 36 (4.2) | 47 (3.7) |
| Iran, Islamic Rep. | 16 (2.2) | 17 (2.5) |
| Ireland | 46 (2.6) | 52 (2.6) |
| Japan | 64 (1.9) | 70 (2.4) |
| Korea | 36 (2.4) | 39 (3.1) |
| New Zealand | 40 (2.6) | 55 (3.6) |
| Norway | 41 (4.1) | 58 (3.1) |
| Portugal | 26 (2.5) | 30 (2.4) |
| ${ }^{+}$Scotland | 42 (2.5) | 55 (2.5) |
| Singapore | 46 (2.2) | 61 (1.9) |
| United States | 54 (2.7) | 68 (1.9) |

Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details):

| Australia | $52(4.1)$ | $59(2.3)$ |
| :---: | :--- | :--- |
| Austria | $38(3.8)$ | $54(3.6)$ |
| ${ }^{1}$ Latvia (LSS) | $23(2.6)$ | $42(3.5)$ |
| Netherlands | $56(2.6)$ | $74(2.6)$ |

Countries Not Meeting Age/Grade Specifications (High
Percentage of Older Students; See Appendix A for Details)

| Slovenia | 44 (3.3) | 49 (2.7) |
| :---: | :---: | :---: |

Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details):

| Hungary | 46 (3.0) | 61 (3.1) |
| :--- | :---: | :---: |
| Unapproved Sampling Procedures at Classroom Level and Not <br> Meeting Other Guidelines (See Appendix A for Details): |  |  |


| I Israel <br> Kuwait <br> Thailand | -- | $51(2.7)$ |
| :--- | :---: | :---: |
|  | -- | $31(2.1)$ |
|  | $30(3.3)$ | $59(2.8)$ |

[^23]
## Table 3.19 Data Representation, Analysis, and Probability

## Percent Correct for Example Item 19 Lower and Upper Grades (Third and Fourth Grades*)



[^24]
## Table 3.20 Data Representation, Analysis, and Probability

## Percent Correct for Example Item 20

Lower and Upper Grades (Third and Fourth Grades*)


[^25]
## International Difficulty Map for Data Representation, Analysis, and Probability Example Items - Lower and Upper Grades (Third and Fourth Grades*)


*Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country.
NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

## What Have Students Learned About Geometry?

The 14 items in the area of geometry represented a variety of content topics. For example, students were asked to recognize basic two-dimensional and threedimensional forms, know basic terms and properties, use visualization to identify equivalence between turned figures, and read coordinate points on a grid.

The data in Table 3.21 reveal that students at both grades had a high degree of success in determining that the plane was located at 2, D on the game board grid (Example Item 21). The international averages of correct responses were $88 \%$ at the fourth grade and $80 \%$ at the third grade. More than $90 \%$ of the fourth-grade students responded correctly in many countries.

Example Item 22 asked students to identify which of four rectangles was not divided into four equal parts. Third graders had more difficulty than fourth graders (international average of $60 \%$ compared to $73 \%$ for fourth graders). However, the data in Table 3.22 reveal that performance was highly variable. For example, more than $80 \%$ of the students at both grades answered this item correctly in Korea and Singapore. In comparison, fewer than $40 \%$ did so in Iran and Kuwait, indicating that such visualization tasks are more prevalent in the primary grade curriculum in some Asian countries than they are in some Middle Eastern countries.

As shown in Table 3.23, Example Item 23 required students to draw what a cut-out shape would look like when it is opened up and flattened out. Students could depict either the cut-out shape or the remaining piece of paper with the shape cut out, but the majority tended to the former. The international averages were $59 \%$ correct at the fourth grade and $45 \%$ at the third grade. In the four Asian countries, $80 \%$ or more of the fourth graders responded correctly, followed by $76 \%$ responding correctly in both England and Scotland.

In Example Item 24, students needed to use their counting and map-reading skills to determine the point where a school was located. As shown in Table 3.24, approximately half were successful internationally ( $54 \%$ of the fourth graders and $43 \%$ of the third graders). Most countries showed an increase in performance between the grades that corresponded to the international results.

Table 3.25 presents the results for Example Item 25, which was based on a figure of a solid cube. Students were asked about the number of edges on the cube. Generally, students at both grades found this a difficult task (international averages of $42 \%$ at the fourth grade and $35 \%$ at the third grade). Approximately one-third of the students at both grades selected 8 (option B) as their answer. At both grades, however, there was quite a range in performance. For example, at the fourth grade, performance ranged from $17 \%$ in Iran and Kuwait to $72 \%$ in Hong Kong. Also, the degree of growth between the two grades varied substantially from country to country.

The item difficulty map for the geometry items is presented in Figure 3.5. It indicates that third-grade students in particular have difficulty with a variety of visualization tasks. Most students at both grades could read the coordinates on a simple grid.

## Table 3.21 Geometry

Percent Correct for Example Item 21
Lower and Upper Grades (Third and Fourth Grades*)


[^26]
## Table 3.22 Geometry

## Percent Correct for Example Item 22

Lower and Upper Grades (Third and Fourth Grades*)


[^27]
## Table 3.23 Geometry

Percent Correct for Example Item 23
Lower and Upper Grades (Third and Fourth Grades*)


[^28]
## Table 3.24 Geometry

## Percent Correct for Example Item 24

Lower and Upper Grades (Third and Fourth Grades*)


[^29]
## Table 3.25 Geometry

## Percent Correct for Example Item 25

Lower and Upper Grades (Third and Fourth Grades*)


[^30]
## International Difficulty Map for Geometry Example Items Lower and Upper Grades (Third and Fourth Grades*)


*Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country. NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

## What Have Students Learned About Patterns, Relations, and Functions?

The 10 items in this content area involved patterns of numbers and shapes, representations of simple numerical situations, and relationships between sequences of numbers. In Example Item 26, students were asked to identify the same pattern as portrayed by two different sets of shapes. The international averages show substantial growth from the third grade ( $61 \%$ ) to the fourth grade ( $72 \%$ ), and indicate that by the seventh and eighth grades most students (about 90\%) can demonstrate this basic skill (see Table 3.26). The increase between the third and fourth grades was particularly notable in Greece, from $29 \%$ to $51 \%$.

Example Item 27 required students to recognize that $4 \times 4$ was less than 17, and that, thus, four would make the number sentence true. Internationally, growth between grades also was substantial on this item, from $55 \%$ to $70 \%$ (see Table 3.27). Thirdgrade students in Korea did particularly well on this item - 88\% correct. The next highest performance at the third grade was in Japan (79\%), Slovenia (75\%), Singapore ( $73 \%$ ), and Latvia ( $72 \%$ ). Such results indicate that representation of numerical situations is introduced quite early in the curriculum of some countries.

Example Item 28 asked students to work out the relationships among several logic statements in order to determine that Henry is older than Peter. As shown in Table 3.28 , results also were relatively stable across countries. However, the international averages of $63 \%$ at the fourth grade and $55 \%$ at the third grade indicate less than the average increase of $13 \%$ between grades shown in Chapter 2.

To receive full credit on Example Item 29, students needed to demonstrate that they understood what to do to get the next number in a subtraction series. For example, they could explain that the numbers were decreasing by 4 , provide the next number or numbers in the series, or give any other type of answer that communicated information about the operation involved. As shown in Table 3.29, the international averages were $57 \%$ at the fourth grade and $41 \%$ at the third grade. There was a great deal of variation across countries, however. For example, at the fourth grade $79 \%$ of the students answered correctly in Singapore and Hungary compared to $12 \%$ in Kuwait.

Example Item 30 required students to identify the relationship between two columns of numbers. The results in Table 3.30 reveal that, on average across countries, only $39 \%$ of the fourth graders and $27 \%$ of the third graders determined that you needed to divide the number in Column A by 5 to obtain the number next to it in Column B. Internationally, about one-fourth of both the third and fourth graders answered that you should subtract 8 from the number in Column A (option B). This response applies only to the first pair of numbers.

Figure 3.6 presents the item difficulty map for the example items in the content area of patterns, relations, and functions. The results indicate that students were more likely to be able to recognize simple patterns and relationships than they were to determine the operations underlying the relationships.

## Table 3.26 Patterns, Relations, and Functions

## Percent Correct for Example Item 26

Lower and Upper Grades (Third and Fourth Grades*)


[^31]
## Table 3.27 Patterns, Relations, and Functions

Percent Correct for Example Item 27
Lower and Upper Grades (Third and Fourth Grades*)


[^32]
## Table 3.28 Patterns, Relations, and Functions

## Percent Correct for Example Item 28

Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 28True statement of ages. |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |  |
| Canada | 59 (2.5) | 68 (2.9) | Henry is older than Bill, and Bill is older than Peter. Which statement must be true? |  |
| Cyprus | 48 (2.7) | 56 (2.9) |  |  |
| Czech Republic | 52 (2.4) | 62 (2.4) |  |  |
| ${ }^{\dagger}$ England | 54 (3.1) | 66 (2.7) |  |  |
| Greece | 54 (3.8) | 54 (3.0) | A. Henry is older than Peter. |  |
| Hong Kong | 65 (2.1) | 74 (2.0) |  |  |
| Iceland | 47 (3.9) | 61 (4.3) | B. Henry is younger than Peter. |  |
| Iran, Islamic Rep. | 41 (2.7) | 41 (2.7) | C. Henry is the same age as Peter. |  |
| Ireland | 61 (2.4) | 66 (2.8) |  |  |
| Japan | 68 (2.1) | 73 (2.1) | D. We cannot tell who is oldest from the information. |  |
| Korea | 80 (1.9) | 86 (1.8) |  |  |
| New Zealand | 57 (3.4) | 64 (2.9) |  |  |
| Norway | 52 (3.2) | 66 (3.2) |  |  |
| Portugal | 46 (3.0) | 54 (2.8) |  |  |
| ${ }^{\dagger}$ Scotland | 58 (2.6) | 65 (2.1) |  |  |
| Singapore | 62 (2.0) | 72 (1.9) |  |  |
| United States | 64 (2.4) | 73 (1.7) |  |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |  |
| Australia | 59 (2.8) | 70 (2.0) |  |  |
| Austria | 52 (3.3) | 57 (3.1) |  |  |
| ${ }^{1}$ Latvia (LSS) | 38 (3.3) | 50 (3.3) |  |  |
| Netherlands | 56 (2.5) | 66 (2.8) |  |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |  |
| Slovenia | 60 (3.1) | 72 (3.2) |  |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |  |
| Hungary | 62 (2.9) | 64 (2.7) |  |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |  |
| ${ }^{1}$ Israel | -- | 68 (3.4) |  |  |
| Kuwait | -- | 43 (2.7) |  |  |
| Thailand | 37 (2.7) | 47 (3.6) |  |  |
| International Average Percent Correct | 55 (0.6) | 63 (0.5) |  |  |

[^33]
## Table 3.29 Patterns, Relations, and Functions

## Percent Correct for Example Item 29 <br> Lower and Upper Grades (Third and Fourth Grades*)

| Country | Percent Correct |  | Example 29Next number in pattern. |
| :---: | :---: | :---: | :---: |
|  | Third Grade | Fourth Grade |  |
| Canada | 38 (2.4) | 57 (2.5) |  |
| Cyprus | 41 (2.6) | 67 (2.1) | These numbers are part of a pattern. |
| Czech Republic | 42 (2.5) | 65 (2.2) | 50, 46, 42, 38, 34, .. |
| ${ }^{+2}$ England | 41 (2.1) | 57 (1.8) |  |
| Greece | 27 (2.2) | 42 (2.6) | What do you have to do to get the next number? |
| Hong Kong | 43 (2.6) | 65 (1.9) |  |
| Iceland | 15 (1.9) | 27 (3.0) | $2 m$ |
| Iran, Islamic Rep. | 14 (1.5) | 22 (1.9) | Answer: 30 $\qquad$ |
| Ireland | 54 (2.8) | 74 (1.9) |  |
| Japan | 40 (1.5) | 58 (1.4) |  |
| Korea | 56 (1.9) | 74 (1.7) |  |
| New Zealand | 34 (1.8) | 48 (2.3) |  |
| Norway | 20 (2.2) | 46 (2.2) |  |
| Portugal | 17 (2.1) | 30 (2.3) |  |
| ${ }^{+}$Scotland | 44 (2.0) | 63 (2.2) |  |
| Singapore | 73 (1.4) | 79 (1.3) |  |
| United States | 40 (1.9) | 61 (2.0) |  |
| Countries Not Satisfying Guidelines for Sample Participation Rates (See Appendix A for Details): |  |  |  |
| Australia | 54 (2.1) | 72 (1.5) |  |
| Austria | 41 (2.8) | 64 (2.5) |  |
| ${ }^{1}$ Latvia (LSS) | 51 (2.7) | 70 (2.5) |  |
| Netherlands | 58 (2.1) | 77 (1.9) |  |
| Countries Not Meeting Age/Grade Specifications (High Percentage of Older Students; See Appendix A for Details): |  |  |  |
| Slovenia | 46 (2.5) | 68 (2.0) |  |
| Countries With Unapproved Sampling Procedures at Classroom Level (See Appendix A for Details): |  |  |  |
| Hungary | 62 (2.3) | 79 (1.7) |  |
| Unapproved Sampling Procedures at Classroom Level and Not Meeting Other Guidelines (See Appendix A for Details): |  |  |  |
| ${ }^{1}$ Israel | -- | 46 (2.9) |  |
| Kuwait | -- | 12 (1.0) |  |
| Thailand | -- | - - |  |
| International Average Percent Correct | 41 (0.5) | 57 (0.4) |  |

[^34]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## Table 3.30 Patterns, Relations, and Functions

## Percent Correct for Example Item 30

Lower and Upper Grades (Third and Fourth Grades*)


[^35]SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

## Figure 3.6

## International Difficulty Map for Patterns, Relations, and Functions Example Items Lower and Upper Grades (Third and Fourth Grades*)



[^36]
[^0]:    The IEA retained about one-third of the TIMSS items as secure for possible future use in measuring international trends in mathematics and science achievement. All remaining items are available for general use.

[^1]:    2 The three-digit item label shown in the lower right corner of the box locating each example item on the item difficulty map refers to the original item identification number used in the student test booklets.

[^2]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^3]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^4]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^5]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^6]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^7]:    *Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country.
    NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

[^8]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^9]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^10]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^11]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^12]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Hungary on Example 10A.

[^13]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Hungary on Example 10B.

[^14]:    *Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country.
    NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

[^15]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^16]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^17]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Japan on Example 13.

[^18]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^19]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^20]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^21]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for England on Example 17.

[^22]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for England on Example 17.

[^23]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^24]:    Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details)
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^25]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^26]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Japan on Example 21.

    SOURCE: IEA Third International Mathematics and Science Study (TIMSS), 1994-95.

[^27]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details)
    National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^28]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^29]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^30]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details)
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Norway on Example 25.

[^31]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^32]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^33]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade.

[^34]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below $65 \%$, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent. A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are unavailable for Thailand on Example 29.

[^35]:    *Third and fourth grades in most countries; See Table 2 for information about the grades tested in each country.
    ${ }^{\dagger}$ Met guidelines for sample participation rates only after replacement schools were included (see Appendix A for details).
    ${ }^{1}$ National Desired Population does not cover all of International Desired Population (see Table A.2). Because coverage falls below 65\%, Latvia is annotated LSS for Latvian Speaking Schools only.
    ${ }^{2}$ National Defined Population covers less than 90 percent of National Desired Population (see Table A.2).
    ( ) Standard errors appear in parentheses. Because results are rounded to the nearest whole number, some totals may appear inconsistent.
    A dash (-) indicates data are not available. Israel and Kuwait did not test at the lower grade. Internationally comparable data are not available for Hong Kong in Example 30.

[^36]:    *Third and fourth grades in most countries; see Table 2 for information about the grades tested in each country. NOTE: Each item was placed onto the TIMSS international mathematics scale based on students' performance in both grades. Items are shown at the point on the scale where students with that level of proficiency had a 65 percent probability of providing a correct response.

