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MATHEMATICS ACHIEVEMENT IN THE
MIDDLE SCHOOL YEARS:
IEA'S THIRD INTERNATIONAL MATHEMATICS
AND SCIENCE STUDY (TIMSS)

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